

1 **LASER SCANNING-BASED DIAGNOSTICS IN THE STRUCTURAL ASSESSMENT OF**
2 **HISTORIC WROUGHT IRON BRIDGES**

3

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25 **ABSTRACT**

26 This paper introduces a workflow to create the geometric documents for conducting finite element
27 based structural assessment of wrought iron bridges using laser scanning data as the input dataset.
28 First, a methodology for identifying actual cross-sections of the bridge components based on a point
29 cloud obtained from a terrestrial laser scanner (TLS) is presented. Next, a non-parametric regression
30 kernel density estimation is employed to determine the overall bridge dimensions to populate a
31 computation model by projecting the position of the web and/or flange surface of the cross-section
32 (appearing as local maximum peaks of a probability density shape). The process is demonstrated with
33 respect to the previously undocumented Guinness Bridge in Dublin, Ireland to determine the bridge's
34 behaviour. The successful generation of this model proves that TLS can surpass other common
35 techniques (e.g. UAV-based images) for acquiring the bridge geometry necessary for reconstructing
36 accurate member cross-sections and overall bridge dimensions, regarding quantity and quality of the
37 data points, and timing. The finite element analysis showed that the bridge currently satisfies both
38 strength and serviceability requirements under self-weight, but would be unlikely to support a new
39 slab and a modern pedestrian load level as per current code requirements for re-opening the bridge.

40

41 **KEYWORDS:** Conservation, Bridges, Maintenance & Inspection.

42

43 **LIST OF NOTATIONS**

DL	dead load
H	distance between the local maximum peaks (LMP) of the probability density shape (PDS) derived from the bottom and top chords
h	bridge height
L	bridge length

LL	live load
M	maximum bending moments
P	maximum axial forces
P_{DL}	applied dead load
P_{LL}	applied live load
S_{11}	principle stress
Δ_{B1}	a distance between a gravity centre of the bottom chord to the LMP of the PDS of the lower parts of the bottom chord
Δ_{B2}	a distance between a gravity centre of the bottom chord to the LMP of the PDS of the upper parts of the bottom chord
Δ_{T1}	a distance between a gravity centre of the top chord to the LMP of the PDS of the lower parts of the top chord
Δ_{T2}	a distance between a gravity centre of the top chord to the LMP of the PDS of the upper parts of the top chord

44

45 **1. INTRODUCTION**

46 The Guinness Bridge in Dublin, Ireland represents an invaluable part of the country's largely
47 disregarded industrial heritage and dates back to the early 1900s. The bridge was the first of its kind
48 in Ireland to carry hydroelectric power and services across the nearby valley to the Farmleigh estate.
49 The bridge has not been used since the 1960s, and no maintenance records were found despite state
50 ownership beginning in 1999. The structure is in an extremely deteriorated state due to half a century
51 of neglect and was nominated World Monument Fund's "Most at Risk" list in 2012. At the time of
52 the nomination, the structure's state and the exact extent of deterioration were both unknown, which
53 precluded the development of a restoration plan and affiliated fundraising. Without a preliminary
54 structural assessment, fundraising and further assessment were stymied. In response, faculty and

55 students at the University College Dublin undertook an evaluation of this late 19th century, wrought
56 iron structure as part of an academic programme. As such, the following serves both as a case history
57 and a framework for the diagnostic assessment of a historic wrought iron bridge using terrestrial laser
58 scanning (TLS) data.

59

60 Visual inspection is a predominant method used in bridge assessment, because the method has the
61 advantage of being simple. It is, however, subjective and highly dependent upon an inspector's
62 experience, especially when working in adverse conditions (e.g. weather and access) (Phares et al.,
63 2004; Zhu et al., 2010). For structures with highly restrictive site access and limited budgets, effective
64 visual inspection with physical inspectors cannot be done. In contrast, TLS is a non-contact
65 measurement method that offers an alternative by acquiring three-dimensional (3D) topographic data
66 on visible surfaces of structural members with millimetre accuracy. Once acquired, TLS data can be
67 processed to generate a permanent record of a structure's status or to report structural deficiencies.
68 This paper describes a methodology developed for the geometric documentation and safety evaluation
69 of this bridge, which could be adapted as a template for other historic bridges.

70

71 **2. BACKGROUND**

72 According to the International Council on Monuments and Sites Charter (ICOMOS) (2003), heritage
73 lies in both the appearance and the integrity of all visible and hidden structural components, as they
74 represent the building technology of a certain time. However, engineers must assess the safety of
75 heritage structures by considering the nature and effects of these structural components (ICOMOS,
76 2003). Ultimately, the structural evaluation of a metal bridge can be done through direct testing,
77 modelling, or a combination of both.

78

79 TLS has been emerging as a non-contact measurement approach to acquire 3D topographic data of
80 objects quickly and accurately. For example, Armesto-Gonzalez et al. (2010) presented a
81 methodology using a combination of TLS and digital image processing to detect damage to the stone
82 ruins of Santo Domingo. In another application, Al-Neshawy et al. (2010) used a FARO LS 880HE80
83 scanner to acquire geometric data of a wall to detect bowing of marble cladding. Other notable case
84 studies employing TLS in heritage building assessment include the works of Camarda et al. (2010)
85 who surveyed the Olympic theatre in Vicenza using photogrammetry and TLS. To obtain a 3D model
86 capturing architectural details and areas with high surface curvatures, a 3D triangulated mesh model
87 of the theatre was created using Geomagic software, which is as an input model for finite element
88 method (FEM) analysis. Similarly, Castellazzi et al. (2015) developed the procedure CLOUD2FEM,
89 which used voxels to represent a point cloud of a structure in order to semi-automatically generate a
90 FEM model of a historic monument building from TLS data based on the earlier introduction of this
91 approach by others (Hinks et al., 2013). More generally, Olsen et al. (2010) proposed a framework
92 for the use of TLS to model existing structures and capture deflections, whilst extending its
93 applicability to damage and volumetric change analysis. Additionally, the authors also addressed
94 parallax and mixed pixel errors that occurred around the edges of the specimen in close range data
95 capture and which required further data filtering.

96

97 Moreover, TLS has also been used widely for heritage structure documentation and assessment (e.g.
98 Armesto-Gonzalez et al., 2010). To such ends, TLS data have been used for geometric reconstruction,
99 as well as the examination of surface damage, deflections, and degradation. In an extensive study of
100 documentation techniques for heritage bridges, Fereshteh (2012) concluded that TLS is ideal where
101 rapid collection of undocumented geometry is needed and/or where the presence of an inspector on
102 the structure itself may pose a safety hazard. That can be seen through the work of Heath and Miller
103 (2014) using TLS to support the assessment of the Iron bridge in Shropshire, UK. In that case, 3D

104 topographic data of the bridge was acquired through 162 TLS scans with a Faro Focus and 47 from a
105 Riegl VZ400. With that data, the authors employed modelling tools from Rhinoceros to generate a
106 3D surface model of the main span. Afterwards, Miller (2015) converted the surface model to a solid
107 model for finite element analysis including the structure's defects (either deleting elements or
108 reducing the stiffness of selected elements). While this helpful example provides some guidance for
109 bridge assessment, generating meaningful surface models of metal bridges from point clouds remains
110 a challenge, particularly with respect to cross-section component identification. Generally, the readers
111 are referred to Truong-Hong and Laefer (2014) for a further discussion of using TLS for bridges,
112 which can be used for deformation measurement; for example to determine a rate of mass loss or
113 detect bridge components' cracking. To understand these issues better and to present a semi-
114 automated method for TLS data processing, the following sections of this paper present a case study
115 of the Guinness Bridge, wherein TLS was used to collect geometric data of the metal bridge to
116 determine the cross-sections of the structural members for structural diagnostics.

117

118 **3. METHODOLOGY**

119 This study aimed to demonstrate how TLS can be used to rapidly and inexpensively collect sufficient
120 data to create a permanent record of a previously undocumented bridge in its current condition
121 without imperilling the site engineers. The project had the further goals of using TLS data to create a
122 geometric model for structural analysis for a safety evaluation. However, since extensive damage of
123 the bridge was apparent from even the most cursory visual inspection, there was concern that the
124 bridge was possibly beyond immediate serviceability. Thus, the evaluation was to be based on a
125 structural analysis conducted on both the strength and serviceability requirements for immediate and
126 long-term scenarios. Visible damage was modelled by assuming reduced stiffness or removal of
127 structural components. The methodology of this investigation involved field documentation of the

128 Guinness Bridge, followed by automatic estimation of primary dimensions of the bridge, and then an
129 estimate of actual cross-sections of the components to create a numerical model with undamaged
130 structural components. Finally, an element-by-element assessment of the structural components under
131 various load scenarios was conducted.

132

133 As part of this process, cross-sections of the bridge components were manually identified based on
134 the point cloud of the cross-section and a library section. The actual section of the component was
135 based on the section in the library that best matched the point cloud in terms of height, width, and
136 cross-sectional area. Notably, no previous records of the geometry and/or performance of the
137 Guinness Bridge were known to exist; therefore, the assessment detailed in this report was based
138 solely on this study using known sections from other projects, as will be described below.

139

140 **3.1 Field Work & Scanning Process**

141 The scan of the Guinness Bridge was conducted using a Leica ScanStation P20, which can acquire
142 up to a million data points per second with an accuracy of 5 mm within the measurement range of 50
143 m [for detailed technical specifications of the scanner see (Truong-Hong et al., 2014)]. A visual
144 survey of the site assisted in the identification of suitable access routes to the structure, selection of
145 viable scan station locations and positions (to maximise data capture), and positional determination
146 of obstructive vegetation.

147

148 Because of the absence of a river bank on the south side, no public access was available there. On
149 the north side significant trees also limited the access. Thus, only two scan positions could be set
150 up—both from the north (Figure 1). Station locations were chosen to maximise a clear line of sight

151 towards the structural members of the bridge and to minimise the angle of incidence. As part of the
152 process, a pair of high definition black and white 6” (15.24 cm) targets were positioned to collect
153 reference data for registering the point clouds from the two scan stations. At each scan station, two
154 levels of scanning were conducted: an overall scan and a detailed scan. The first had a sampling step
155 of 12.5mm for overall geometrical data of bridge members. The second for recording detailed cross-
156 sections had a 1.6mm sampling step at the measurement range of 10m. Scanning at each position
157 required around 30 minutes for data acquisition.

158

159 **3.2 Data Processing**

160 Following data collection, processing of the raw point cloud was undertaken to extract the required
161 information for creating 3D solid models of the bridge for documentation and a subsequent numerical
162 model. This was done using a combination of AutoCAD with the plug-in CloudWorx (Leica
163 Geosystems AG, 2016) for cross-section identification, and novel algorithms developed by the
164 authors for overall dimension estimation. After data acquisition, the point clouds from the multiple
165 TLS scan stations were imported into Leica Cyclone V.9.1 (Leica Geosystems AG, 2014) for co-
166 registration using the two common artificial targets. A total of 15.33 million points were collected,
167 with 9.57 million of which describing the bridge (Figure 2). Following co-registration of the two
168 scans, irrelevant data points (e.g. points of the trees) were manually removed using the software’s
169 cropping tools.

170

171 To be able to assess the structure numerically, a 3D geometric model of the bridge was required.
172 Obtaining this involved two main steps: (1) identifying the cross-section of each structural member
173 from a point cloud; and (2) determining the overall dimensions of the bridge consisting of its total
174 length, width, and height, as well as the distance between individual deck beams and struts.

175

176 In Step 1, an actual cross-section of a structural component was identified by comparing the section-
177 based point cloud to a library of sections. The library was created from the ‘Historical Structural
178 Steelwork Handbook’ (Bates, 1991). As a formal standardization of wrought iron sections had yet to
179 fully exist within the industry, this use of steel sections may have contributed to small discrepancies,
180 however, since no quantifiable documentation of the bridge existed, this proxy had to be used.

181

182 When exporting a point cloud from Leica Cyclone V.9.1 (Leica Geosystems AG, 2014) into
183 AutoCAD using the plug-in CloudWorx (Leica Geosystems AG, 2016), working with an entire point
184 cloud is difficult because (1) the AutoCAD programme requires intensive hardware (i.e. RAM and
185 graphics card) to handle and visualise a massive data point, and (2) distinguishing individual
186 components within the full point cloud is visually challenging. Additionally, the bridge’s components
187 are repetitive in nature. Thus, the point cloud of each structural component was imported into the
188 AutoCAD programme separately for identifying the cross-section, and the process was applied across
189 all of bridge’s components individually. Notably, since the point cloud density is proportional to the
190 offset distance, the structural component closest to the scanner (having the highest point density) was
191 used for the initial identification of the repeated member’s cross-section.

192

193 To obtain the actual cross-section of the structural elements, a local coordinate system was defined
194 for the structure by defining a User Coordinate System (UCS) in the AutoCAD programme, where
195 the z-axis was parallel to the longitudinal direction of the component and its cross-section lay on the
196 x-y plane. Following alignment, the point cloud of the cross-section of a given structural component
197 was cropped using the ‘Clipping’ tool in Leica CloudWorx (Leica Geosystems AG, 2016). An
198 iterative procedure for section identification was applied. The process is illustrated in Figures 3 and

199 4, being applied to the bottom and top chords, respectively. Photos of the structural members further
200 supported the identification of the components (Figure 3a and 4a).

201

202 After projecting the point cloud of the cross-section onto the x-y plane, an outline of the section was
203 first sketched manually using in-built AutoCAD tools (Figure 3b and 4b). Using photos as
204 supplemental information, the individual components of each cross-section were identified. A
205 possible section shape for each component was then estimated. This was necessary due to the highly
206 complex, composite geometry of the pieces. For example, the bottom and top chord were made from
207 an L section and multiple plates (Figure 3c and 4c).

208

209 Next a cross-section from the section library with the closest dimensions to that of the point cloud
210 was inserted into AutoCAD and manually mapped onto the estimated section. Figures 3d and 4d
211 depict the final cross-sections derived from the library for the bottom and top chords, respectively.
212 The same process was then applied to the top chords, bottom chords, ties, sway bracing, lateral cross-
213 bracing, lattice web elements, deck, arch, end posts, and plate girders. Differences between the
214 estimated cross-sectional areas and the sections in the library are shown in Table 1. The deviations
215 ranged between 1.36% and 30.65%, but most differed by less than 10%.

216

217 Step 2 was an automatic procedure to estimate the primary dimensions of the bridge to create a
218 numerical model appropriate for FEM analysis. The dimensions included the bridge's overall length,
219 width, and height, as well as the separation distances between the individual deck beams and the
220 individual struts (Figure 5). The dimensions were reported as centre-of-gravity to centre-of-gravity
221 of the elements, as opposed to the clearance. To achieve these objectives, based on data point
222 distributions, a statistical model was developed to estimate the position of the web and/or flange

223 surface of the section, which was an important component for determining those dimensions. This
224 was done using non-parametric regression, kernel density estimation (KDE) [Laefer and Truong-
225 Hong, 2017] to detect the primary surfaces (web and flanges) of the structural member, which
226 appeared as local maximum peaks (LMPs) of a probability density shape (PDS). The member
227 dimensions were then derived from the positions of the LMPs. Details of the method for dimension
228 estimation to create the 3D computational model are explained below.

229

230 The deck beam was extracted (red points in Figure 5a) from the bridge point cloud (Figure 2). The
231 PDS was then generated from the point cloud's y-coordinates using the empirically selected
232 bandwidth of 10 times the sampling step along the longitudinal direction. The PDS results are shown
233 in Figure 5b. From the LMPs positions describing the location of the deck beams, the distance
234 between beams was determined to be 0.960 m, with a standard deviation (std) of 0.026 m. Notably,
235 since the first deck beam was embedded into the rock face, the point cloud of this beam was not
236 available, but the distance from the second deck beam to the end post was approximately 0.750 m, as
237 measured from the data points of the second deck beam and from one of the end posts. Measurement
238 was done via an AutoCAD plug-in tool with Leica CloudWorx (Leica Geosystems AG, 2016).

239

240 Similarly, the point clouds of the struts were also extracted (in blue in Figure 5a). In Figure 5c, the
241 LMPs of the PDS generated from the y-coordinates of the points demonstrated that the distance
242 between the struts can be divided into three groups: (1) the first bay of the north and south sides with
243 an average distance of 4.379 m (std = 0.073 m); (2) a pair of bays at the middle with a distance of
244 3.604 m (std = 0.004 m); and (3) other elements with a distance of 3.830m (std = 0.032 m).

245

246 Based on the distances between the deck beams and between the struts above, the bridge length was
247 calculated. The inner 55 deck beams had an average distance between them of 0.960 m, while the
248 outermost pairs of deck beams at each end were 0.750 m apart. Thus, the lower portion of the bridge
249 was calculated to be approximately 54.30 m long. However, based on the number of struts and their
250 offsets from each other (using an identical procedure), the upper portion of the bridge was only 54.27
251 m long. Since the difference in bridge length was only 3cm, the disparity was not considered critical
252 for the analysis, and the length generated based on the deck beams (54.30 m) was used to create the
253 computational model, as it was closer to the scan data and, thus, considered more accurate.

254

255 To estimate the bridge width, the bottom and top chords were extracted separately (see green and
256 pink points, respectively, in Figure 5a). The segment located between the two adjacent deck beams
257 was automatically extracted based on the LMP of the PDS. From pairs of bottom (or top) chords, a
258 PDS based on the x-coordinate of the data points was then generated to predict the locations of each
259 web (Figure 5e). The distance between the webs was considered as the bridge width for the segment.
260 The average bridge width was 4.257 m (std = 0.036 m).

261

262 Similarly, the point cloud of a segment involving the bottom and top chords on the same vertical truss
263 plane was used to predict the bridge height. The PDS generated from the z-coordinate of the data
264 points enabled positional prediction of the flanges of the cross-section of the chords (Figure 5e).
265 Subsequently, the distance between the flanges of the cross-sections of the bottom and top chords
266 could be determined. However, since the bridge height (h) from the numerical model was the distance
267 between the gravity centres of the bottom and top chords, the distance in Figure 6e had to be adjusted
268 by the distance from the gravity centre of the cross-section to the flanges as the LMPs. For example,
269 for Case 1, the amount of 0.0485 m ($h = H - \Delta_{B1} + \Delta_{T1}$) had to be subtracted, while the distance in

270 Case 2 the value was 0.2283 m ($h = H - \Delta_{B1} - \Delta_{T2}$) [Figure 5e]. The resulting average bridge height
271 was 3.709 m (std = 0.016 m).

272

273 **3.3 Computational analysis**

274 A final 3D geometric model of the bridge, which also integrated a severe state of deterioration derived
275 from a visual inspection [Truong-Hong and Laefer, 2015a; Truong-Hong and Laefer, 2015b], is
276 shown in Figure 6. Thus, an FEM assessment was performed to examine the strength and
277 serviceability requirements of the bridge under different scenarios. Using the overall bridge
278 dimensions and element cross-sections acquired in the previous section, an as-designed model of the
279 bridge was created in SAP2000 V.17 (CSI, 2014), which initially assumed no deterioration. The
280 bridge components including bottom and top chords, deck beams, lattice, sway bracing, arch, and end
281 posts were modelled by frame elements. However, deck beams, lattice, sway bracing, arch, and end
282 posts (Figure 6) having rivet connections at the ends were modelled as truss elements, by releasing
283 the bending moment at both ends and torsion moment at one end. Finally, since lateral bracing
284 provides stability against lateral loads, it acts in tension only and was, thus, modelled with a cable
285 element. The ‘Section Designer’ extension of SAP2000 V.17 was used to define composite, unique
286 cross-sections of the structural components. In such cases, the program merged multiple, individual
287 sections of the component into the single geometry. Hinged and roller supports were, respectively,
288 applied for the boundary conditions of North and South abutments (Figure 6). Material properties
289 specified in Table 2 were assigned to the bridge’s elements.

290

291 The aims of the FEM analysis were to assess strength and service requirements of the bridge structure
292 in its current condition and then to answer the question of whether a new deck slab could be rebuilt
293 safely to serve the community for pedestrian usage. Although a visual inspection recorded extensive

294 damage in the deck beams, including surface loss due to corrosion and deformation, those damages
295 could not be fully documented under current access limitations (Figure 6). Notably, connections
296 between some deck beams and the bottom chord were welded, thereby showing some post-
297 construction maintenance. As such, the present condition was analysed under four scenarios: Case
298 1: the as-designed bridge model without any damage; Case 2: Case 1 but with the stiffness of moment
299 of inertia of all deck beams reduced by 50% to represent corrosion; Case 3: Case 1 but with selected
300 deck beams removed (Figure 7)—deck beam removal was based on assumed surface loss due to
301 severe corrosion (derived from ground-based inspection images); and Case 4: Case 1 but with a new
302 deck slab similar to the original (Figure 8a). For this case, a UB 127x76x13 (British steel section)
303 was assumed as a stringer for a 10 cm deep ash wood deck slab.

304

305 Since Cases 1-3 had no slab, the bridge was only subjected to self-weight, which was defined by the
306 cross-sectional area, the lengths of the structural members, and a mass density. In Case 4, the bridge
307 was subjected to both dead load (DL) and live load (LL). The dead load from the slab system
308 (stringers and slab) was computed from the self-weight of the stringer at 13 kg/m and ash wood, with
309 a mass density by 710 kg/m³. In addition, for LL, a modern pedestrian load of 4.3 kN/m² equivalent
310 to 90 psf was selected according to AASHTO (2012). The concentrated loads from the slab system
311 transferred to the deck beam are shown in Figure 8b. However, since the distances between the deck
312 beams differ, the dead load (P_{DL}) and live load (P_{LL}) were applied to the deck beams in accordance
313 with their spacings (0.3kN and 1.4kN for the first and last beam, 0.7kN and 3.5kN for the second and
314 the penultimate deck beams, and 0.8 kN and 4.1kN for others) [Figure 8b]. Finally, load combinations
315 under strength I (STR1) and service I (SER1) according to AASHTO (2012) were used in this
316 assessment. For STR1, the load factors for DL and LL were respectively 1.25 and 1.75, while in SER1
317 all load factors were 1.0.

318

319 **4. RESULTS**

320 Results of the major internal forces involving axial force and bending moment under STR1 from
321 Cases 1-4 are depicted in Figures 9 and 10 for the bottom and top chords, while the summary of the
322 maximum and minimum of load (P) and bending moments (M) are reported in Tables 3 and 4. The
323 results showed that the axial force and bending moment changed slightly in Cases 1-3, whereas the
324 maximum difference of axial force and bending moment found in the bottom chord were respectively,
325 5 kN (Case 2 vs. Case 3) and 0.1 kNm (Case 2 vs. Case 3). In Case 3, some deck beams were removed,
326 thus, the internal forces were slightly reduced, because the bridge was only subjected to self-weight.
327 In Case 4, when the new slab was installed and the bridge was subjected to a pedestrian load, the
328 internal forces were increased significantly. As an example, the maximum axial force in the bottom
329 chord increased by more than 4.5 times, from 465 kN (Case 1) to 2138 kN (Case 4), with a similar
330 increase in the bending moment (from 4.2 kNm in Case 1 to 19.8 kNm in Case 4). The same increase
331 also occurred in the primary structural members like top chords, single and double lattices, and end
332 posts. Of special note was the increase in the deck's bending moment from 0.9 kNm in Case 1 to 19.5
333 kNm in Case 4, while, the internal forces in the secondary structures (i.e. struts, sways and arches)
334 changed only slightly.

335

336 An important issue in checking the capacity of the bridge is to examine the principal stress of the
337 structural members. A summary of the minimum and maximum principal stresses of the structure is
338 provided in Table 6, which were computed from the internal forces at sections of the structural
339 components and the section properties. For Cases 1-3, both the compressive and tensile principal
340 stresses of the structural members were under the allowable strength of wrought iron. For example,
341 the maximum compressive principal stress in the top chord was 52 N/mm² (nearly 64% of the
342 allowable compressive strength of 81 N/mm²) for the top chord in Case 1, while the maximum tensile
343 principal stress was 37 N/mm² (around 60% of the allowable compressive strength of 61 N/mm²) for

344 the bottom chord. However, in Case 4, the loading on structural members increased significantly and
345 exceeded the allowable strength in terms of the principal stress in the bottom and top chords, deck
346 beam, single lattice, double lattice and end-post. Exceedance occurred in the bottom chord (the
347 maximum tensile stress by 169 N/mm²). In the top chord, the maximum compressive stress was 239
348 N/mm². As such, the bridge structure would not satisfy modern strength requirements if the slab was
349 re-built and subjected to modern pedestrian loads, even in an undamaged state. As such the study
350 demonstrated that with its current condition, the slab most definitely cannot be rebuilt to modern
351 standards to serve the community without significant structural retrofit.

352

353 In terms of deformation analysis, the bridge's deflections were described as the vertical displacement
354 of the bottom chord (Figure 11). This was examined by comparing the allowable deflection, $L/500$
355 ($L = 54.3$ m is the span length in meter) according to AASHTO (2012). The maximum deflections
356 from Cases 1-3 were mostly the same, with the maximum deflections less than 30 mm. In Case 4 with
357 the new slab, deflection increased to 42.3 mm corresponding to $1/1285L$ under the DL and a further
358 67.1 mm with the addition of the LL, which was slightly larger than the maximum allowable
359 deflection of 108.6 mm. This demonstrates that the bridge in an undamaged state with a new slab
360 subjected to modern pedestrian loads would not satisfy the deformation limitation requirements and
361 would exceed the principal stress limit, which raises the question of the appropriateness of applying
362 modern concepts to historic structures. In this case, given the extreme deterioration of many of the
363 sections, the bridge is clearly at risk with respect to its continued existence under its current self-
364 weight.

365

366 **5. DISCUSSION**

367 In the absence of site-specific documentation, period building standards, and codes, this project was
368 heavily guided by assumptions and educated judgments, as must typically happen in the assessment
369 of historic bridges (Fernandez, 2017). The fabric of the bridge was previously recorded by the
370 Department of Arts, Heritage, and the Gaeltacht (2012) as cast iron of unknown specification.
371 However, during this study, the authors found reason to believe that the structure was composed of
372 wrought iron. This was based on the visual survey conducted, in which the dimensional characteristics
373 of cast iron, wrought iron, and steel as listed in the CIRIA (1994) were compared. Specifically, typical
374 features of the physical elements, such as the small, equal flange I deck beam sections, and the small
375 plate sections riveted together with rounded corners to form the chords were not in agreement with
376 characteristic shapes of cast iron elements. Furthermore, according to an initial numerical analysis
377 (not reported herein) based on the originally reported cast iron designation of the bridge and standard
378 properties for that material, most of the bridge's structural members had principal stresses exceeding
379 the allowable stress when the undamaged version of the bridge was subjected to its self-weight. Those
380 numerical results did not coincide with the visual inspection. As such, the model was rerun using
381 typical material attributes of historic wrought iron sections and affiliated material properties.

382

383 Following the re-examination of the results using the characteristics of wrought iron, the scanned
384 model reflected the visual observations with respect to extant cross-section shapes and in situ
385 performance. Since access to the structure was restricted and line of sight was limited, the scan data
386 for the bridge was acquired from only two positions but provided information beyond what was
387 available via direct visual inspection in terms of element lengths and cross-sectional areas. This
388 demonstrated the inherent usefulness of TLS for data collection for creating a numerical model. The

389 ability to do such documentation in only an hour also argues for the superiority of using TLS in terms
390 of both data accuracy, cost, and schedule compared to traditional means or even those from an
391 unmanned vehicle. For example, UAV-based imagery, which is a prominent method for bridge
392 inspection, has an average error of about 15 mm (Palmer et al, 2015) and requires extensive
393 processing to generate a point cloud from the raw imagery. With such an error budget, deploying
394 image-based point cloud for reconstructing 3D models of metal members is problematic (Laefer and
395 Truong-Hong, 2017). Instead, the cross-sections generated herein had an average difference between
396 the estimated and recorded library sections of only 285.9 mm² (std = 314.1 mm²). Importantly
397 however, as with all line-of-sight technologies, mixed pixels, registration errors, and missing data
398 may cause section misidentification and increase errors in determining the overall dimensions of the
399 bridge.

400

401 Finally, without the TLS data, remotely estimating the dimensions of the members safely, cost
402 effectively, and with reasonable accuracy would have been extremely difficult and time consuming.
403 That said, the data accuracy and level of detail collected could be improved by the following actions:
404 1) conducting the scan when all foliage is off the trees; 2) increasing the number of scans conducted
405 (where possible); 3) widening the range of scan locations (where possible); 4) scanning the structure
406 from all faces including from the river and the air (e.g. using UAV-based laser scanning or TLS
407 integrated with a boat); and 5) increasing the scanning resolution.

408

409 As reported in Tables 5 and 6, when the actual cross-section without damage and wrought iron
410 material properties were used in the model and the bridge was subjected to self-weight loading, as in
411 Case 1, the highest principal stresses generated from the numerical modelling (52 N/mm² in
412 compression and 37 N/mm² in tension) were smaller than the allowable stress. The maximum
413 displacement under self-weight found at mid-span was 29.431 mm. However, the as-designed

414 structure was not representative of the current bridge. Visual assessment confirmed excessive material
415 damage from corrosion (Figure 6), which can cause stiffness reduction of elements such as the deck.
416 Two additional numerical analyses (Case 2 and 3) were conducted to consider potential element
417 deficiencies: either decay or loss of functionality. Those results showed that neither the stiffness
418 reduction of the deck beams nor the removal of several deck beams negatively impacted the primary
419 structures (e.g. bottom and top chords, and lattices) in terms of the principal stress and deflection.
420 However, when considering the recommendation by Gagg and Lewis (2011) and Beal (2011) that
421 aging and material degradation could further reduce the existing structure's ultimate strength by half,
422 this would have limited the compressive and tensile strength of the wrought iron to 41.5 N/mm^2 and
423 30.5 N/mm^2 , respectively. In that case, the principal stresses in both the bottom and top chords, and
424 the end-post would exceed the reduced allowable strength. For example, in Case 2, the compressive
425 principal stress in the top chord and end-post were respectively 52 N/mm^2 and 49 N/mm^2 with no
426 safety factor incorporated into this value.

427

428 To consider reopening the bridge to serve the local community, a new wooden slab (and additional
429 LL) would be needed. Case 4 considered this in the ideal scenario of no degradation with respect to
430 structural members but with modern pedestrian loading requirements. In that case, the numerical
431 results showed that in the primary members (e.g. bottom and top chords, deck beam and lattices)
432 loading demands would have increased by nearly 3 times for the compressive stress (239 N/mm^2 vs.
433 81 N/mm^2 in a top chord) and 2.7 times for the tensile stress (169 N/mm^2 vs. 61 N/mm^2 in a bottom
434 chord). In this case, the maximum principal stress in most structural components exceeded the
435 strength of the wrought iron, but the principal stresses were mainly caused by LL. For example, in
436 the bottom chord, the maximum tensile principal stresses consisted of 52 N/mm^2 from DL and 116
437 N/mm^2 from LL. However, the principal stress due to DL is around 86% of the tensile strength (52

438 N/mm² vs. 61 N/mm²). Thus, reopening the bridge to serve the community cannot be safely
439 undertaken at this time under current codes.

440

441 **6. CONCLUSIONS**

442 This investigation highlighted the beneficial role of terrestrial laser scanning technology in
443 documenting and assessing a historic wrought iron bridge, especially where the geometry is otherwise
444 unrecorded. In the presented case study of the Guinness Bridge, geometries of the bridge components
445 were acquired from only two positions (and both from the same abutment). However, this was
446 sufficient for identifying cross-sections of all components and the overall dimensions of the bridge to
447 create a numerical model from the resulting point cloud. The success of the proposed method proved
448 that TLS can surpass other common techniques (e.g. UAV based images) for acquiring geometric
449 models of the bridge in terms of quantity and quality of the data points, and timing. However, with
450 restricted access to the bridge allowing only two scanning positions, the acquired data points may not
451 record the deficiencies of components farther from the scanner, which limits the reliability of the
452 modelling.

453

454 The geometries and cross-sections based on the TLS data agreed with a published historic record,
455 thereby confirming the suitability of the technology and the authors' conclusion that the structural
456 material was wrought iron, as opposed to the officially recorded cast iron designation. A successful
457 methodology for generating a 3D model can be applied to other similar structures. Subsequent simple
458 modelling showed that the bridge, in its current geometry and assuming original material properties,
459 is likely to be able to satisfy both strength and serviceability requirements under self-weight without
460 its deck, thereby demonstrating that further intervention and inspection of the bridge can be done
461 safely without concern for progressive collapse. However, in terms of the possibility of re-opening

462 the bridge for community service, the analysis concluded that the stress demands in the primary
463 structures greatly exceeded the allowable strength.

464

465 To adequately assess the structure, material testing using non-invasive methods is needed, along with
466 detailed modelling of each damaged member. Irrespective of the limitations of this study and the
467 ultimate fate of the bridge, TLS documentation can provide a detailed record of the structure for future
468 assessments both in terms of cross-sectional geometry and overall dimensions for numerical
469 modelling.

470

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474

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- 548

549 **TABLES**550 **Table 1.** Summary of element cross sections relating scanned and standard dimensions

Element	Estimated cross-sectional area (mm ²)	Standard cross-sectional area (mm ²)	Absolute error (mm ²)	Relative error (%)
Bottom Chord	14800	13800	-1000	-7.25
Top Chord	9170	9700	530	5.45
Deck beam	4230	4150	-080	-1.93
Arch	2120	1940	-180	-9.28
Tie	2260	2420	160	6.61
Sway	1050	930	-120	-13.27
Lateral bracing	0520	480	-040	-7.64
Double lattice	2430	1860	-570	-30.65
Single lattice	3630	3680	050	1.36
End post	3200	3070	-130	-4.23

551

552 **Table 2.** Material properties of wrought iron

Aspect	Wrought Iron	Reference
Young modulus of Elasticity, E (N/mm ²)	1.99 x10 ⁵	Friedman (2010)
Poisson's ratio, ν	0.278	Rattan (2011)
Tensile strength, σ_t (N/mm ²)	61	Bates (1991)
Compressive strength, σ_c (N/mm ²)	81	Bates (1991)
Mass density, W (kg/m ³)	74	Doran (2013)

553

554 **Table 3.** Maximum axial forces (P) and bending moments (M) in each type of structural member

Structural Member	Case 1		Case 2		Case 3		Case 4	
	P (kN)	M (kNm)	P (kN)	M (kNm)	P (kN)	M (kNm)	P (kN)	M (kNm)
Bottom chord	465	4.2	465	4.2	460	4.1	2138	19.8
Top chord	-35	2.5	-35	2.5	-33	2.5	-168	11.1
Deck beam	0	0.0	0	0.9	0	0.9	0	19.5
Strut	1	0.4	1	0.4	1	0.4	1	0.4
Sway	-0	0.1	0	0.1	0	0.1	0	0.1
Single lattice	47	1.0	47	1.0	46	1.0	225	3.0
Double lattice	1	0.4	1	0.4	1	0.4	11	0.8
End post	-34	0.7	-34	0.7	-33	0.6	-155	3.2
Arch	-0	0.3	-0	0.2	-0	0.3	-0	0.2

555

556

557 **Table 4.** Minimum axial forces (P) and bending moments (M) in each type of structural member

Structural Member	Case 1		Case 2		Case 3		Case 4	
	P (kN)	M (kNm)	P (kN)	M (kNm)	P (kN)	M (kNm)	P (kN)	M (kNm)
Bottom chord	35	-0.7	35	-0.7	35	-0.6	156	-3.2
Top chord	-467	-0.5	-467	-0.5	-462	-0.5	-2172	-2.1
Deck beam	-0	-0.5	-0	-0.5	-0	-0.5	-0	-1.5
Strut	0	-0.0	0	-0.0	0	-0.0	-0	-0.2
Sway	-1	0.0	-1	0.0	-1	0.0	-1	0.0
Single lattice	-0	-0.4	-0	-0.4	-0	-0.4	12	-0.2
Double lattice	-47	-0.3	-47	-0.3	-46	-0.3	-211	-0.2
End post	-95	-0.7	-95	-0.7	-93	-0.7	-431	-3.2
Arch	-1	-0.1	-1	-0.1	-1	-0.1	-1	-0.2

558

559 **Table 5.** Principal stress (S_{11}) in each type of structural members

Structural member	min S_{11} (N/mm ²)				max S_{11} (N/mm ²)			
	Case 1	Case 2	Case 3	Case 4	Case 1	Case 2	Case 3	Case 4
Bottom chord	-1.7	-1.7	-1.2	-17.2	36.6	36.6	36.2	168.9
Top chord	-51.8	-51.8	-51.3	-238.5	-1.0	-1.0	-1.0	-7.4
Deck beam	-4.0	-4.0	-4.0	-88.0	4.0	4.0	4.0	88.0
Strut	-24.0	-24.0	-24.0	-23.6	24.2	24.2	24.2	24.0
Sway	-7.5	-7.5	-7.5	-7.6	6.3	6.3	6.3	6.3
Single lattice	-6.0	-6.0	-6.0	-22.3	20.5	20.5	20.3	68.9
Double lattice	-37.6	-37.7	-37.3	-126.7	20.9	20.9	20.8	51.3
End post	-46.6	-49.1	-46.0	-199.2	-4.5	-5.3	-3.9	-31.5
Arch	-12.5	-12.3	-12.5	-12.0	12.0	11.8	12.0	11.4

560

561 **Table 6.** Summary table of model performance

Structural scenario	Load		Material Capacity 100%		Material Capacity 50%	
	DC	LL	Principal Stress	Deflection	Principal Stress	Deflection
Case 1	Yes	None	OK	N/A	Exceeded	N/A
Case 2	Yes	None	OK	N/A	Exceeded	N/A
Case 3	Yes	None	OK	N/A	Exceeded	N/A
Case 4	Yes	Yes	Exceeded	Yes	Exceeded	Exceeded

562

563

564 **FIGURE CAPTIONS**

565 **Figure 1.** Positions of scan stations and targets

566 **Figure 2.** Point cloud of the Guinness Bridge after registration and removal of irrelevant points

567 **Figure 3.** Evolution of point cloud to a final cross-section of the bottom chord (Note: value in
568 brackets is in Imperial units). a) Photo of a bottom chord; b) Sketch of a cross-section outline based
569 on a point cloud; c) Estimate of a cross section based on the sketched section; d) Finalised cross-
570 section based on a library entry

571 **Figure 4.** Evolution of point cloud to a final cross-section of the top chord (Note: value in brackets
572 is in Imperial units). a) Photo of a bottom chord; b) Sketch of a cross-section outline based on a
573 point cloud; c) Estimate of a cross section based on the sketched section; d) Finalised cross-section
574 based on a library entry

575 **Figure 5.** A point cloud of segments for determining primary dimensions of the bridge based on
576 LMPs of PDS from KE. a) Point clouds of structural components used to estimate primary
577 dimensions of the bridge for creating the computational model; b) Distances between deck beams
578 (half of the bridge from the north side) estimated from the point clouds of the deck beam; c)
579 Distances between struts estimated from a point cloud of struts; d) Bridge width predicted from the
580 point cloud of pairs of bottom or top chords; a distance between the center of gravity to the LMPs;
581 e) Bridge height predicted from the point cloud of the bottom and top chords Note: red circles
582 denote LMPs of PDS generated by KE

583 **Figure 6.** FEM model of Guinness Bridge

584 **Figure 7.** Removal of deck beam No. 3-6 and 45-47 from north to south sides

585 **Figure 8.** A new slab design. a) New slab; b) Loads transfer from the new slab

586 **Figure 9.** Axial forces and bending moment in the bottom chord of the bridge a) Axial forces; b)
587 Bending moment

588 **Figure 10.** Axial forces and bending moment in the top chord of the bridge a) Axial forces; b)

589 Bending moment

590 **Figure 11.** Deflection of the bottom chords due to dead loads

591

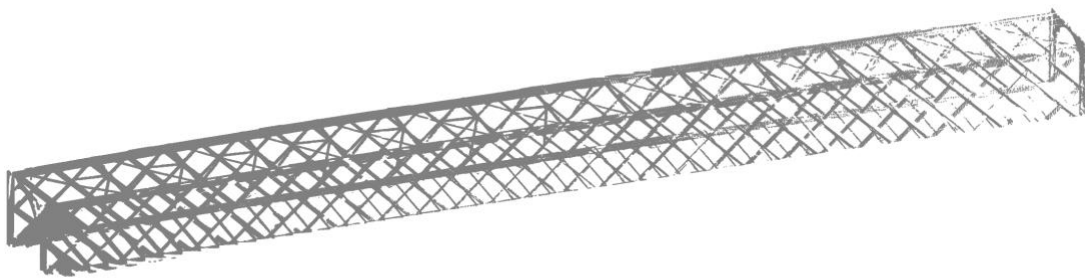
592 **FIGURES**



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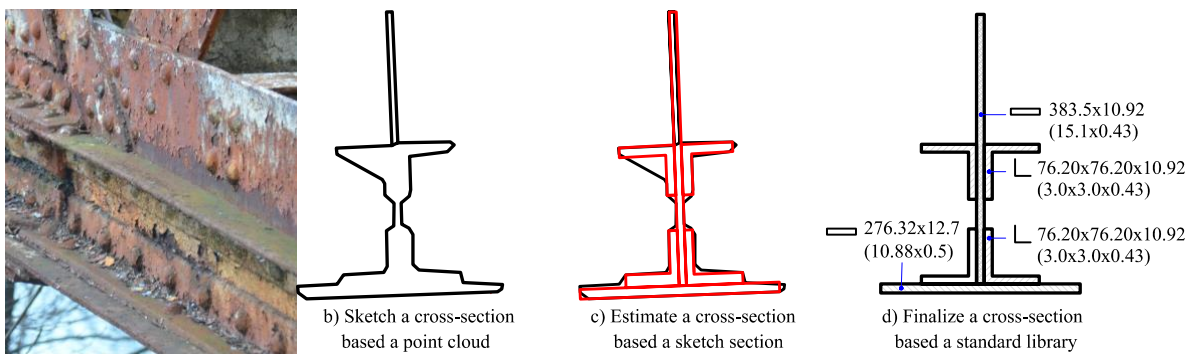
Figure 1. Positions of scan stations and targets



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Figure 2. Point cloud of the Guinness Bridge after registration and removal of irrelevant points



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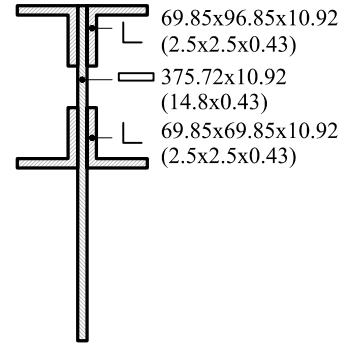
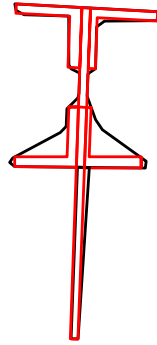
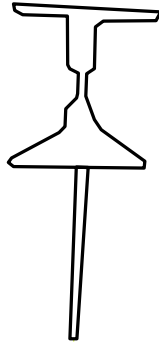
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Figure 3. Evolution of point cloud to a final cross-section of the bottom chord (Note: value in brackets is in Imperial units). a) Photo of a bottom chord; b) Sketch of a cross-section outline based on a point cloud; c) Estimate of a cross section based on the sketched section; d) Finalised cross-section based on a library entry



b) Sketch a cross-section based a point cloud

c) Estimate a cross-section based a sketch section

d) Finalize a cross-section based a standard library

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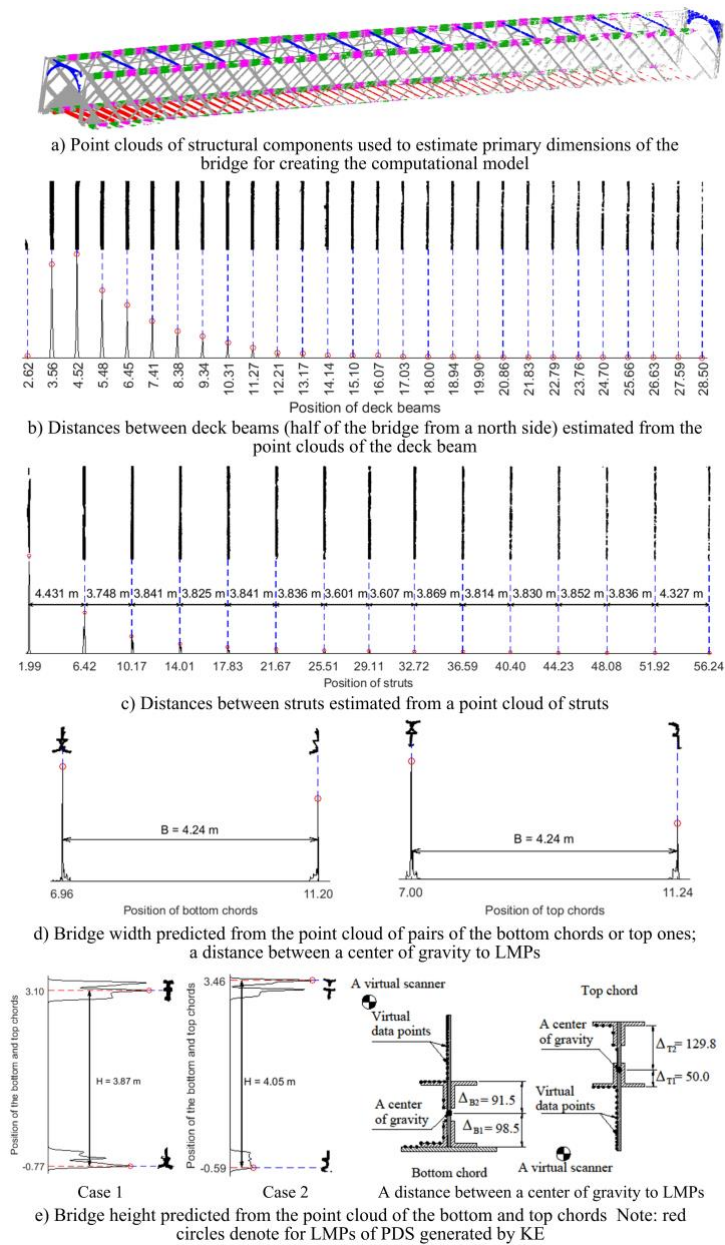
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Figure 4. Evolution of point cloud to a final cross-section of the top chord (Note: value in brackets is in Imperial units). a) Photo of a bottom chord; b) Sketch of a cross-section outline based on a point cloud; c) Estimate of a cross section based on the sketched section; d) Finalised cross-section based on a library entry



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Figure 5. A point cloud of segments for determining primary dimensions of the bridge based on

LMPs of PDS from KE. a) Point clouds of structural components used to estimate primary

dimensions of the bridge for creating the computational model; b) Distances between deck beams

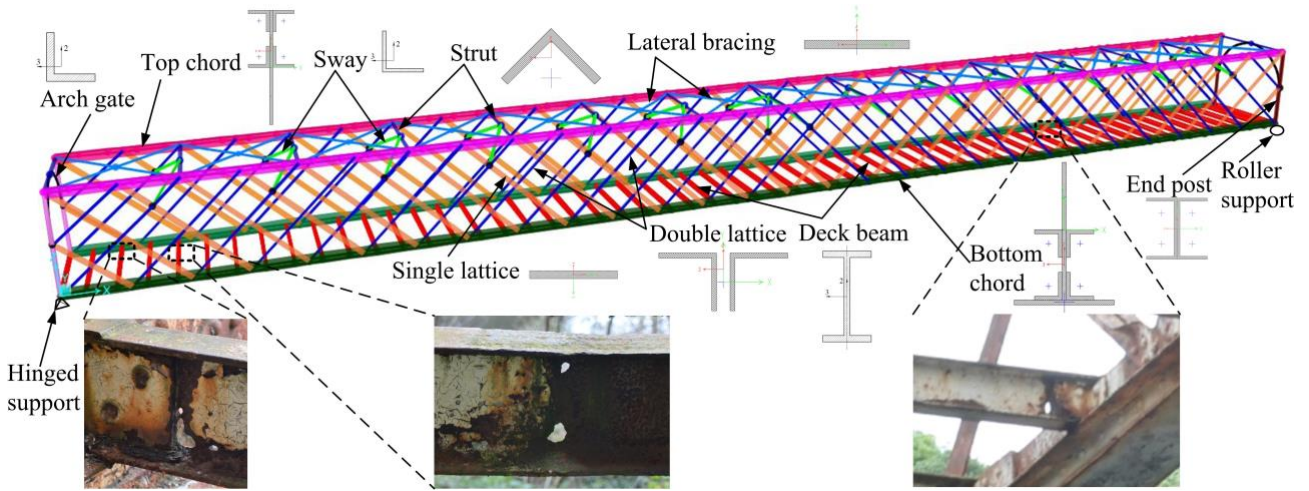
(half of the bridge from the north side) estimated from the point clouds of the deck beam; c)

Distances between struts estimated from a point cloud of struts; d) Bridge width predicted from the

point cloud of pairs of bottom or top chords; a distance between the center of gravity to the LMPs;

e) Bridge height predicted from the point cloud of the bottom and top chords. Note: red circles

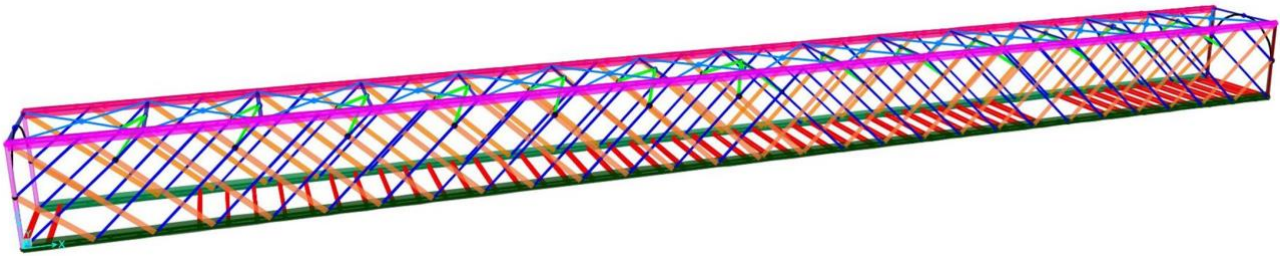
denote LMPs of PDS generated by KE



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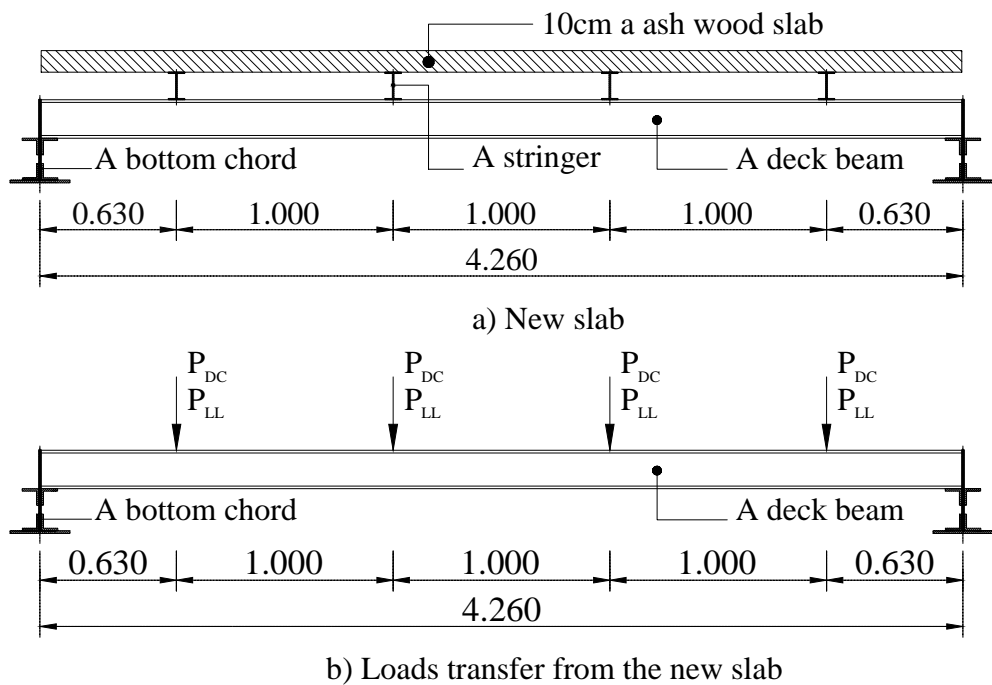
Figure 6. FEM model of Guinness Bridge



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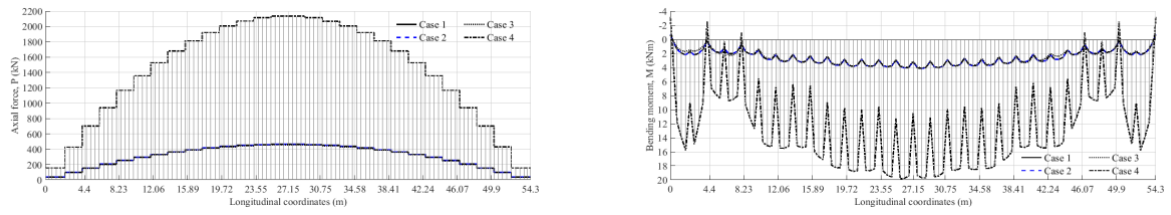
Figure 7. Removal of deck beam No. 3-6 and 45-47 from north to south sides



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Figure 8. A new slab design. a) New slab; b) Loads transfer from the new slab

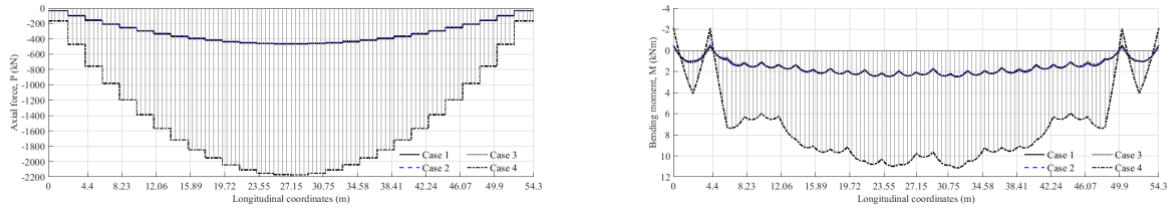


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623 **Figure 9.** Axial forces and bending moment in the bottom chord of the bridge a) Axial forces; b)

624

Bending moment

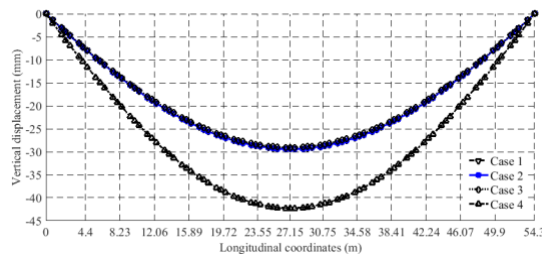


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626 **Figure 10.** Axial forces and bending moment in the top chord of the bridge a) Axial forces; b)

627

Bending moment



628

629

Figure 11. Deflection of the bottom chords due to dead loads

630